

SOV 124 58 10 11-4

# The Minimum Weight of Anisotropic Shells

non-negative scalar factor. On the assumption that a shell of minimum weight enters the state of creep instantly and in its entirety, the author deems  $\Delta$  to be constant from which (1) leads to the condition

$$D/\Delta = \text{const} \quad (2)$$

of the constancy of the rate of dissipation per unit volume of the bearing volume. It is observed that this condition was derived from other considerations for the problem of the axisymmetric flexure of a circular isotropic plate by Freiburger and Tekinalp (Freiburger, W. and Tekinalp, B., J. Mech. and Phys. Solids, 1956, Vol. 4, Nr. 4, pp. 294-299; RZhMekh, 1958, Nr. 7, abstract 7992). A system of equations for the solution of shells and plates is written out. Ideas are suggested on the possibility of application of conditions of type (2) to the case of a shell consisting of a single layer. In conclusion, the "problem of optimum nonuniformity of the material" is posed, i.e., that of how the law of change in the creep limits of the material must be given relative to the coordinates so that all points of a solid will go instantaneously into the state of creep. By way of example, problems are solved for the optimum nonuniformity of a cylindrical tube and a spherical vessel subject to uniform internal pressure. Three unknowns—the radial and tangential stresses and the yield point—are found from Card 2/3

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three equations (the equilibrium equation, the condition of strain compatibility, and the yield condition). It should be noted that the problem is meaningless in the rigid plastic formulation, while in the elastic-plastic formulation the problem of optimum nonuniformity of material is trivial. Its solution is obtained immediately after the yield equation for the stress components found for the elastic problem is written. In particular, the examples examined by the author can provide nothing beyond the familiar Lamé equations. The author's equations for radial stresses do, in point of fact, agree with those of Lamé. The equations for the yield point are also correct. However, the equations for tangential stresses are erroneous in both of the examples stated.

G. S. Shapiro

Card 3/3

MIKELADZE, M.Sh.

AUTHOR  
TITLE

SOKOLOWSKIY, V.V., MIKELADZE, M.Sh.,  
IX. International Congress on Applied Mechanics.

PA - 2622

PERIODICAL

(IX mezhdunarodnom Kongressye po prikladnoy mekhanike - Russian)  
Vestnik Akademii Nauk SSSR, 1957, Vol 27, Nr 3, pp 101-103, (U.S.S.R.)  
Received 5/1957 Reviewed 6/1957

ABSTRACT

The International Society for studies in theoretical and applied physics organizes scientific congresses every 4 years. At present about 30 countries are members of the society, among them since a short time ago, also the Soviet Union. More than 500 scientists from 30 countries delivered lectures on the IX. International congress which took place from September 5. - 13. The following 4 lectures were delivered at the full session. "Electrodynamics of high Velocities" by P. German (France), "New Horizons in Mechanics of hard Bodies" by P. Hill (England), "Sips" by M. Davidson (USA), and "The nonlinear phenomena of Vibration caused in Hard Bodies" by G. Mettles (German Federal Republic). Work was carried out mainly in two sections. "Mechanics of Liquids and Gases" and "Mechanics of Hard Bodies". Each of these sections was subdivided into subsections in which scientific lectures were delivered. The greatest attention was devoted to problems of hydromechanics and gas dynamics dealt with by the first section. About 270 lectures were delivered in the various other section, mainly on the theory of plastics. The following subjects were dealt with by scientists from the USSR. "The Gasdynamical Theory of Novae" (Sydov, L.I.), "The Theory of the Hardness of Plates and Layers" (Vasov, V.), "Problems of Gliding"

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IX. International Congress on Applied Mechanics.

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(Rabotnov, Yu.N.), "Investigations of Tensile Strength in Plastics"  
(Sokolovskiy, V.V.), "Two Theories on Gas Flows" (Sryetyenskiy, L.I.),  
"Dynamics of inelastic threads of variable Length" (Savin, G.N.)  
"Integral Equations of the Thin Wing" (Madam Krasil'shchikova, E.A.)  
etc. In connection with an analysis of the work carried out this  
congress the opinion was expressed that there were too few plenary  
sessions.

ASSOCIATION

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Card 2/2

Library of Congress

MIKELADZE, M.Sh.

Plastic shells of uniform strength. Soob. An Gruz. SSR 25  
no. 4:391-398 0 '60. (MIRA 14:1)

1. Akademiya nauk Gruzinskoy SSR, Tbilisskiy natsional'nyy  
institut im. A.M. Razmadze. Predstavleno akademikom N.I.  
Muskhelishvili.

(Elastic plates and shells)

report presented at the 1st All-Union Congress of Theoreticians and Applied Mechanics,  
Moscow, 27 Jan - 1 Feb 60.

164. A. D. Lektorskiy (Moscow): On space bending of columns in the elastoplastic range.
165. V. A. Lomov (Moscow): Vibration of thin membranes.
166. V. A. Lomov (Moscow): Plasticity of solids under constant loading.
167. A. I. Lomov (Moscow): Some problems of nonstationary flow in incompressible viscoelastic (Maxwellian) liquids.
168. A. I. Lomov, N. D. Bulgarov (Moscow): Some problems of steady flow in an incompressible viscoelastic (Maxwellian) liquid.
169. A. A. Lomov (Leningrad): The generalization of the torsion theory of thin-walled bars.
170. A. A. Lomov, V. V. Pavlovskiy (Leningrad): The development of a theory.
171. N. A. Lomov (Leningrad): Plastic flow of directly plastic under tension and bending of compression and bending.
172. A. A. Lomovskiy (Leningrad): Torsion of an anisotropic bar.
173. A. D. Lomovskiy (Leningrad): Free vibrations and stability of stationary and prestressed elastic restrained beams.
174. A. Lomovskiy (Leningrad): Supplementation of rules for construction of design layers.
175. V. V. Lomovskiy (Leningrad): On the application of matrix methods to the solution of large sets of linear equations of elasticity theory.
176. A. I. Lomovskiy (Leningrad): On the solution of linear equations for the stability of equilibrium of rigid bodies.
177. A. A. Lomovskiy (Leningrad): Large deformations of elastic shells.
178. A. A. Lomovskiy (Leningrad): Methods for the solution of the problem of admissible states of stress in shells of reinforced concrete.
179. A. A. Lomovskiy (Leningrad): Analysis of an anisotropic shell under external load under an arbitrary load applied to a plate.
180. A. A. Lomovskiy (Leningrad): On the experimental study of stresses in plates and shells.
181. A. A. Lomovskiy (Leningrad): Creep stresses and regimes of high polymers.
182. A. A. Lomovskiy (Leningrad): Vibrations of non-circular cylindrical shells.
183. A. A. Lomovskiy (Leningrad): Some problems of combined loading of elastic-plastic shells.
184. A. A. Lomovskiy (Leningrad): The influence of structural anisotropy in concrete on its strength.
185. A. D. Lomovskiy (Leningrad): Investigation of the state of stress in concrete under the action of arbitrary loads under dynamic loading.
186. A. A. Lomovskiy (Leningrad): Solving the plane elastic problem for anisotropic bodies by reduction to the problem of linear mapping with "displacement".
187. A. I. Lomovskiy, N. A. Lomovskiy (Leningrad): The stability of a cylindrical shell in bending.
188. V. A. Lomovskiy (Leningrad): Stress and strain in naturally deformed bars.
189. V. A. Lomovskiy (Leningrad): The problems of nonuniform transformation and plane elasticity for the interior of an infinite number of holes.
190. A. A. Lomovskiy (Leningrad): On the design of thick and infinitely thin plates under arbitrary loads.
191. A. A. Lomovskiy (Leningrad): Vibrations of a curved bar in an elastic medium and in elastic supports.
192. A. A. Lomovskiy (Leningrad): An experimental study of basic creep laws for soils.
193. A. A. Lomovskiy (Leningrad): On statistically equivalent loading.
194. A. A. Lomovskiy (Leningrad): Contribution to the theory of plastic shells under strength.
195. A. A. Lomovskiy (Leningrad): On the bending of a simply supported parallel-plate plate.
196. A. A. Lomovskiy (Leningrad): Evaluation of the mechanical properties of elastic, viscoplastic materials in homogeneous stress-state under external shearing stress.

MIKELADZE, M.Sh.

Equally stable layered structures. Soob. AN Gruz. SSR 26 no.4:397-  
404 Ap '61. (MIRA 14:8)

1. Tbilisskiy matematicheskiy institut imeni A.M. Razmadze  
AN Gruzinskoy SSR i Gruzinskiy politekhnicheskiy institut imeni  
V.I. Lenina. Predstavleno chlenom-korrespondantom AN GruzSSR  
O.D. Oniashvili.

(Elastic plates and shells)

MIKELADZE, M. SH.

Theory of perfectly plastic thin shells.  
A survey of Soviet Contributions.

Report to be submitted for the Shell Structures, International  
Association for (IASS) Symposium on Non-Classical Shell Problems  
Warsaw, Poland, 2-5 Sept 63



MIKELADZE, M.Sh., doktor tekhn. nauk, prof.; ONIASHVILI, O.D., red.;  
~~GIORGADZE, O.N., red.izd-va;~~ BOKERIYA, E.N., tekhn.red.

[Statics of anisotropic plastic shells] Statika anizotrop-  
nykh plastichnykh obolochek. Tbilisi, Izd-vo AN Gruz.SSR,  
1963. 117 p. (MIRA 16:8)  
(Elastic plates and shells) (Plasticity)

MIKELADZE, M.Sh.

Semimomentless theory of cylindrical plastic shells. Dokl.  
AN SSSR 154 no.2:298-299 Ja'64. (MIRA 17:2)

1. Gruzinskiy politekhnicheskii institut im. V.I. Lenina.  
Predstavleno akademikom A.Yu. Ishlinskim.

L 31001-55 EWT(d)/EWT(m)/EWP(w)/EWA(d)/EWP(v)/EWP(k)/EWA(h) Pf-4/Feb EM/RM

ACCESSION NR: AP5006990

S/0198/65/001/001/0062/0069

AUTHOR: Mikeladze, M. Sh. (Tiflis)

26

25

B

TITLE: Basic equations of semimembrane theory of orthotropic plastic cylindrical shells

26

SOURCE: Prikladnaya mekhanika, v. 1, no. 1, 1965, 62-69

TOPIC TAGS: plastic shell design, semimembrane shell theory, orthotropic plastic shell, cylindrical shell

ABSTRACT: The general semimembrane theory of plastic cylindrical shells is elucidated, assuming anisotropy of their material. The theory is based on the evident fact that a pure plastic state of a shell is possible if there is proper variation in the shell thickness; therefore, for a given loading of a cylindrical shell a thickness is sought for which the yield condition will be satisfied at every point of the shell. Such an approach to the problems provides for a certain optimality of their solutions. The formulas describing the plastic state of stress over the thickness of orthotropic cylindrical shells and the plasticity conditions are discussed. General solving equations for a

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ACCESSION NR: AP5006990

cylindrical shell are obtained from the equilibrium equation of a shell element, and the boundary conditions for various shell supports are established. Solving equations for particular cases (circular shell, shallow shell, arbitrary-cross-section shell) are derived. Basic equations of cylindrical uniform-strength shells are discussed, and the principles of designing the sandwich shells are outlined. Orig. art. has: 9 formulas. [VK]

ASSOCIATION: Gruzinskiy politekhnicheskii institut (Georgian Polytechnic Institute)

SUBMITTED: 10Mar64

ENCL: 00

SUB CODE: AS

NO REF SOV: 008

OTHER: 004

ATD PRESS: 3198

Cord 2/2

L 33968-65 EWT(d)/ENT(m)/EWP(w)/ENA(d)/EWP(v)/EWP(k)/ENA(h) Pf-4/Peb EM  
 ACCESSION NR: AP5007266 8/0198/65/001/002/0040/0047

AUTHOR: Mikeladze, M. Sh. (Tiflis)

TITLE: Evaluating the carrying capacity of shallow shells of rotation and of prolate-curved round plates  $\lambda$

SOURCE: Prikladnaya mekhanika, v. 1, no. 2, 1965, 40-47

TOPIC TAGS: shell theory, shell structure, yield strength, centrifugal force, bending moment, stress load  $\lambda$

ABSTRACT: The carrying capacity of shallow shells of rotation and prolate-curved slabs was investigated analytically. The governing equations are written in cylindrical coordinates, two for equilibrium conditions and one for the Mises' yield condition

$$\frac{d}{dr}(rT_r) - T_\theta = 0;$$

$$\frac{d}{dr}(rM_r) - M_\theta - (rT_r)\frac{d\epsilon(r)}{dr} = - \int_0^r p r dr;$$

Card 1/3  $\frac{1}{h^2}(T_r^2 - T_r T_\theta + T_\theta^2) + \frac{12}{h^2}(M_r^2 - M_r M_\theta + M_\theta^2) = \sigma_s^2$ . The condition for static stress

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ACCESSION NR: AP5007266

is given by  $T_r = T_\theta = N$  (constant). The condition for a kinematically possible solution is expressed by  $\int w dF = \int D dF$ , where  $w$  is the deflection rate,  $F$  is the mean shell surface area, and  $D$  is the rate of dissipation of mechanical energy. A shell of constant thickness is considered with a mean surface  $\xi(r) = f \left[ 1 - \left( \frac{r}{b} \right)^2 \right]$ .

under a uniformly distributed load  $p$ . Using the above static-kinematic solution, the following lower and upper bounds for carrying capacities are derived:

$$p = \sqrt{p_m^2 + \left( \frac{4\sigma_y h f}{b^2} \right)^2} \quad p < p_m + \frac{8\sigma_y h f}{\sqrt{3}b^2} \quad . \quad \text{A similar analysis for the prolate-curved}$$

slab yields as an external boundary an ellipse with semi-axes 1 and 1.24. As a practical application the carrying capacity of a disk is considered subject to a tensile centrifugal force as well as an axial bending load. The internal and external bounds are then described by the curves  $\bar{\omega}^4 + \bar{p}^4 = 1$  and  $\bar{\omega}^4 + (1.01)^4 \bar{p}^4 = (1.12)^4$ ,

respectively. As a final application, the disk is assumed to be subject to a radial bending moment uniformly distributed along the outside periphery. Orig. art. has: 49 equations and 3 figures.

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L 33968-65

ACCESSION NR: AP5007266

ASSOCIATION: Gruzinskiy politekhnicheskiy institut (Georgian Polytechnical Institute)

SUBMITTED: 10Mar64

ENCL: 00

SUB CODE: AS,NP,ME

NO REF SOV: 003

OTHER: 000

Card 3/3

E 43885-65 EWA(h)/EWP(k)/EWT(d)/EWT(m)/EWA(d)/EWP(w)/EWP(v) PF-4/Feb EM

ACCESSION NR: AP5006850

S/0023/65/160/004/0789/0791

AUTHOR: Mikeladze, M. Sh.

TITLE: Theory of gently-sloping anisotropic plastic shells

SOURCE: AN SSSR. Doklady, v. 160, no. 4, 1965, 789-791

TOPIC TAGS: shell theory, anisotropic shell, plastic shell, gently sloping shell, equal strength shell, equal stress shell, orthotropic shell

ABSTRACT: The theory is developed with two aims in mind: determine the carrying capacity of gently sloping orthotropic shells, and find rational forms for their construction. The theory is based on the assumptions usually employed for elastic shells and on an approximate rigid-plastic computation scheme, in accordance with which both the elastic and the elastic-plastic parts of the shell are assumed to be rigid, meaning that the plastic state is assumed to be produced instantaneously through the thickness of the shell. The carrying capacity of the shell is determined with the aid of theorems formulated and proved by the author for orthotropic shells elsewhere (Statika anizotropnykh plastichnykh obolochek [Statics of Aniso-

Card 1/2



L 43885-65

ACCESSION NR: AF5006850

[tropic Plastic Shells], AN GruzSSR, 1963; Izv. AN SSSR, OTN, no. 1, 1957). The theory is applied to determine the carrying capacity of a gently-sloping shell hinged along a contour and subject to only a uniform vertical load. The question of equal-strength (and minimum weight) shell under the influence of specified forces is also considered. It is shown that for an isotropic shell with fixed hinged edges subject to only vertical load the equal-strength construction is also an equal-stress construction. This paper was presented by A. Yu. Ishlinskiy. Orig. art. has: 7 formulas.

ASSOCIATION: Gruzinskiy politekhnicheskii institut im. V. I. Lenina (Georgian Polytechnic Institute)

SUBMITTED: 20Jul64

ENCL: 00

SUB CODE: AS

NR REF SOV: 006

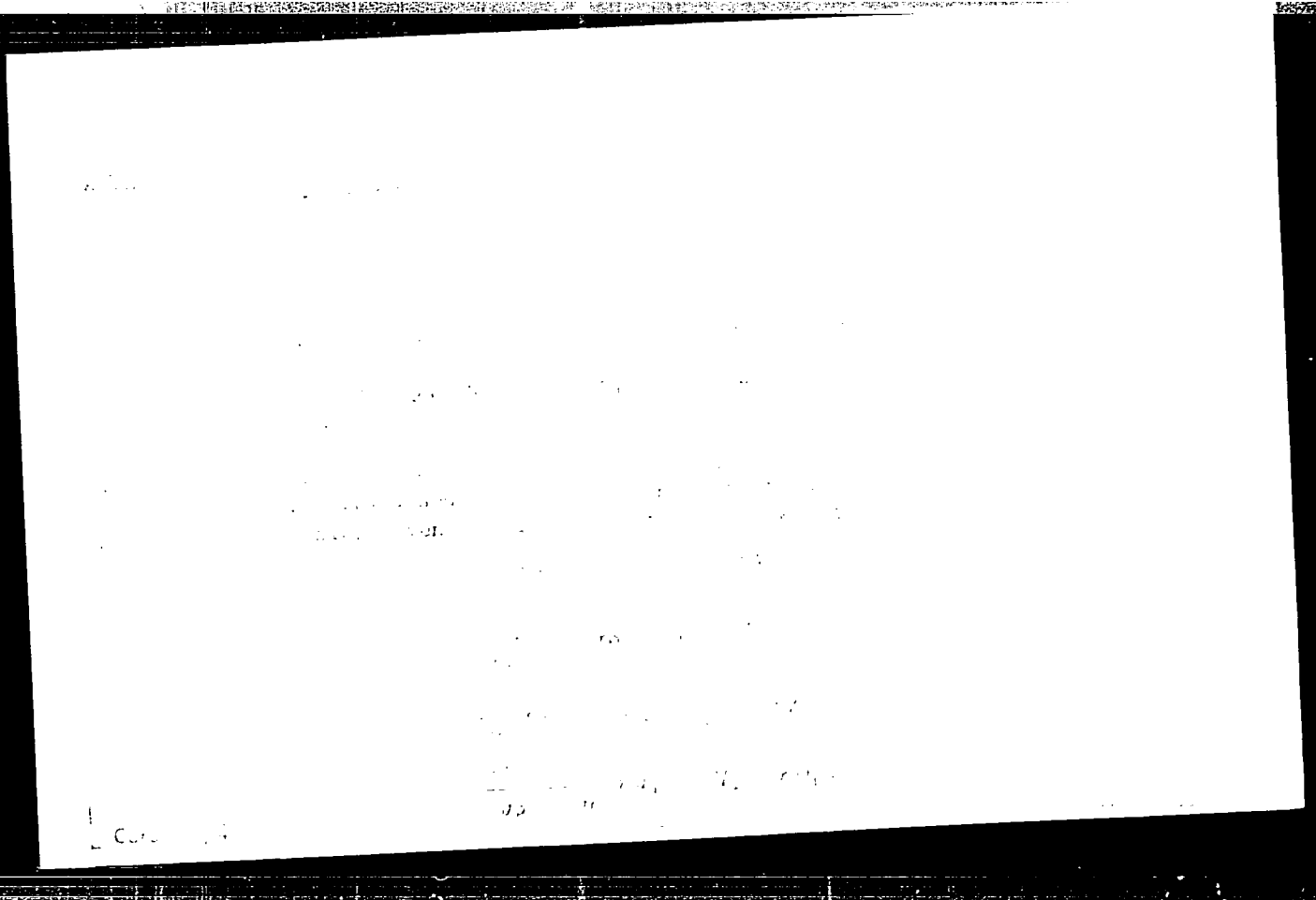
OTHER: 006

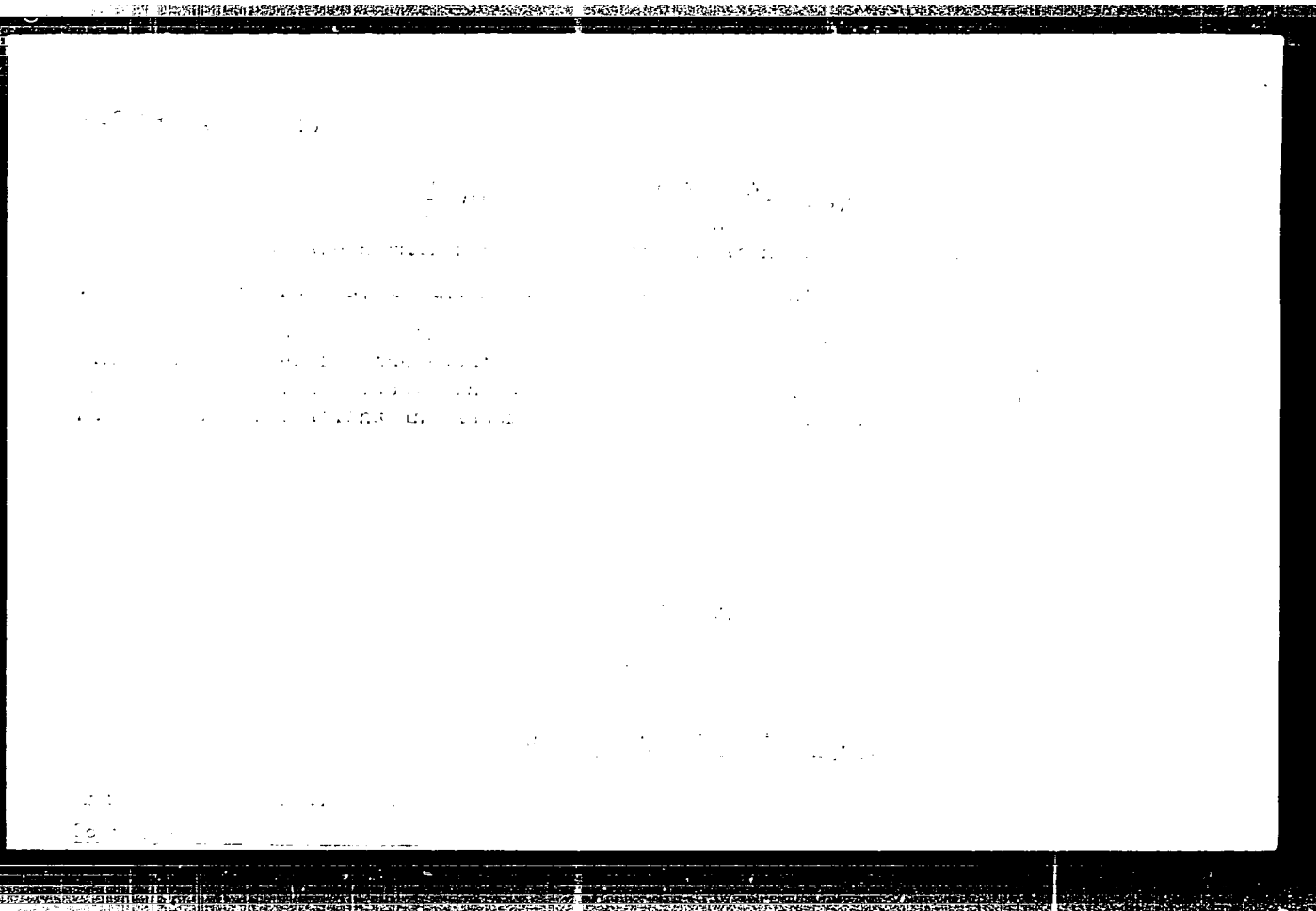
Card 2/2 MB

MIKELADZE, M.Sh. (Tbilisi)

Basic equations of the semi-zero-torque theory of cylindrical  
orthotropic plastic shells. Prikl. mekh. 1 no.1:62-69 '65.  
(MIRA 18:5)

1. Gruzinskiy politekhnicheskiy institut.





"APPROVED FOR RELEASE: 07/12/2001

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CIA-RDP86-00513R001033910020-2

APPROVED FOR RELEASE: 07/12/2001

CIA-RDP86-00513R001033910020-2"

1. MAKSHIN, A. V. STAVROV, A.
2. SP (500)
4. Construction Industry - Finance
7. Days in which to lower construction costs, in, 1953.

9. Monthly List of Russian Accessions, Library of Congress, June 1953. Unclassified.

BRAZHNIK, Viktoriya Ivanovna; MIKELADZE, Pavel Vyacheslavovich;  
FOMICHEV, Vasilii Ivanovich; USPENSKIY, V.V., kand. ekon.  
nauk, nauchnyy red.; MORSKOY, K.L., red.; MIKHEYEVA, A.A.,  
tekhn. red.

[Planning and financing capital construction; practice of  
the Dnepropetrovsk Economic Council] Planirovanie i finansirovanie kapital'nogo stroitel'stva; opyt Dnepropetrovskogo  
sovnarkhoza. Moskva, Gosstroizdat, 1963. 76 p.

(MIRA 16:8)

(Dnepropetrovsk Province--Construction industry--Finance)



MIKELADZE, R.M.

Studying the typology and dynamics of the alpine vegetation of  
Southern Ossetia. Soob.AN Gruz.SSR 23 no.4:457-464 0 '59.  
(MIRA 13:5)

1. Akademiya Nauk Gruzinskoy SSR, Institut botaniki, Tbilisi.  
Predstavleno akademikom N.N.Ketskhoveli.  
(Ossetia--Alpine flora)

IKHLEBZ, I. M. Genl. 191 341 -- " For the study of the Alpine covers of South  
Osetiya." Tbilisi, 1960 (Tbilisi State Univ in Stalin. Chair of Botany).  
(KL, 1-61, 188)

-11-

MIKELADZE, R.M.

Contribution to the study of the alpine carpets of southern Ossetia.  
Probl. bot. 5:170-181 '60. (MIRA 13:10)

1. Botanicheskiy institut AN GruzSSR, Tbilisi.  
(Ossetia--Alpine flora)



MSLADL, Sh. Ye.

On Nov. 12, 1951, the following information was received from the Ministry of Internal Affairs of the USSR:

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4. On Nov. 12, 1951, the following information was received from the Ministry of Internal Affairs of the USSR:

5. On Nov. 12, 1951, the following information was received from the Ministry of Internal Affairs of the USSR:

U koraku kh. funktsii, otdelivshiesia s differentsiala, i na krasnoy str. 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81, 82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 121, 122, 123, 124, 125, 126, 127, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 188, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 202, 203, 204, 205, 206, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 219, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 234, 235, 236, 237, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 250, 251, 252, 253, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 265, 266, 267, 268, 269, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 331, 332, 333, 334, 335, 336, 337, 338, 339, 340, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 365, 366, 367, 368, 369, 370, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 383, 384, 385, 386, 387, 388, 389, 390, 391, 392, 393, 394, 395, 396, 397, 398, 399, 400, 401, 402, 403, 404, 405, 406, 407, 408, 409, 410, 411, 412, 413, 414, 415, 416, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 428, 429, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 451, 452, 453, 454, 455, 456, 457, 458, 459, 460, 461, 462, 463, 464, 465, 466, 467, 468, 469, 470, 471, 472, 473, 474, 475, 476, 477, 478, 479, 480, 481, 482, 483, 484, 485, 486, 487, 488, 489, 490, 491, 492, 493, 494, 495, 496, 497, 498, 499, 500, 501, 502, 503, 504, 505, 506, 507, 508, 509, 510, 511, 512, 513, 514, 515, 516, 517, 518, 519, 520, 521, 522, 523, 524, 525, 526, 527, 528, 529, 530, 531, 532, 533, 534, 535, 536, 537, 538, 539, 540, 541, 542, 543, 544, 545, 546, 547, 548, 549, 550, 551, 552, 553, 554, 555, 556, 557, 558, 559, 560, 561, 562, 563, 564, 565, 566, 567, 568, 569, 570, 571, 572, 573, 574, 575, 576, 577, 578, 579, 580, 581, 582, 583, 584, 585, 586, 587, 588, 589, 590, 591, 592, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 607, 608, 609, 610, 611, 612, 613, 614, 615, 616, 617, 618, 619, 620, 621, 622, 623, 624, 625, 626, 627, 628, 629, 630, 631, 632, 633, 634, 635, 636, 637, 638, 639, 640, 641, 642, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 672, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 696, 697, 698, 699, 700, 701, 702, 703, 704, 705, 706, 707, 708, 709, 710, 711, 712, 713, 714, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 730, 731, 732, 733, 734, 735, 736, 737, 738, 739, 740, 741, 742, 743, 744, 745, 746, 747, 748, 749, 750, 751, 752, 753, 754, 755, 756, 757, 758, 759, 760, 761, 762, 763, 764, 765, 766, 767, 768, 769, 770, 771, 772, 773, 774, 775, 776, 777, 778, 779, 780, 781, 782, 783, 784, 785, 786, 787, 788, 789, 790, 791, 792, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 807, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 835, 836, 837, 838, 839, 840, 84

50: Mathematics in the USSR, 1917-1947  
edited by Kurosh, A. G.,  
Markushevich, A.I.,  
Rashevshiy, P.K.  
Moscow-Leningrad, 1948



MIKELADZE, Sh. Ye.

Numerical Methods for the Integration of Partial Differential Equations

Izd-vo Akad. Nauk SSR, 1936.



IKEL, M. E., CH. E.

"On the Solution of Marginal Value Problems with the Differential Method," Dok. AN, 28,  
No. 5, 1940.  
Geo-organic Dept. of UdSSR Acad. of Scholars. Inst. of Math. Tbilissi. cl<sup>o</sup>40-.

MIKELADZE, Sh. Ye. Continued

Formuly kvadratur s raznost yami. Tbilisi, Soobshch, AN Gr SSR, 3 (1942), 1001-1003.  
O formulakh mekhanicheskikh kubatur, soderzhashchikh chastnyye proizvodnyye integriruemoy  
funktsii. Tbilisi, Soobshch. AN Gr SSR, 4 (1943), 297-300.  
O formulakh kvadratur. DAN, 49 (1945), 167-168.  
Teoriya i praktika interpolirovaniya (na gruz. yaz.) Tbilisi, (1946), 1-393.

SO: Mathematics in the USSR, 1917-1947  
edited by Kurosh, A.G.,  
Markushevich, A.I.,  
Rashevskiy, P.K.  
Moscow-Leningrad, 1948

MIKELADZE, Sh. Ye.

"The Problem of Longitudinal Bending of Rectilinear Rods within the Limits of Elasticity,"

Trudy Math. Inst. im Razmadze, Acad. Sci. Geo SSR, Vol 12, 1943  
(Soob. AN Geo SSR, Vol 7, No 3, 1946.

*Mikheledze, S.*

*Mikheledze, S. An approximate method for the integration of the differential equation for the bending of a beam. Bull. Acad. Sci. Georgian SSR [Sobremennaya Akad. Nauk Gruzinskoi SSR] 6, 97-104 (1945). (Georgian. Russian summary)*

*The method of finite differences is used to integrate numerically the differential equation for the deflection of a beam with variable modulus of rigidity.*

*L. S. Sakofukoff (Los Angeles, Calif.).*

Source: *Mathematical Reviews,*

Vol.

No.

6

MIKHELADZE, S. I.

Mikheladze, S. I. On the subtabulation of mathematical tables. *Dokl. Akad. Sci. Georgian SSR [Sobremennia Akad. Nauk Gruzinskoi SSR]* 6, 397-405 (1945). (Georgian and Russian)

The author considers the problem of the  $m$ -fold subtabulation of a table of  $f(x)$  originally given for  $x=a+kh$  ( $k=0, 1, 2, \dots$ ) to obtain a table for the arguments  $x=a+kh_1$ , where  $h_1=h/m$ . Formulas are given for forward, backward and central differences with remainders after  $r$  terms expressed in terms of the  $(r+1)$ th derivative of  $f(x)$ .

D. H. Lehmer (Berkeley, Calif.).

Source: *Mathematical Reviews*,

Vol. 1 No. 5

*Michelsdy, S.*

Michelsdy, S. On a process of interpolation for functions of two variables. *Bull. Acad. Sci. Georgian SSR [Sovietia Akad. Nauk Gruzinsk SSR]* 6, 503-509 (1945). (Georgian. Russian summary)

The author presents the usual two-variable interpolation formula in terms of differences for a right triangular array of points in the  $(x, y)$  plane. The formula is given in four different forms corresponding to the four possible orientations of the right triangle, i.e., right angle in the N.W., N.E., S.W. or S.E. corner. (P. E. Hine (Corvallis, Ore.))

2

Source: Mathematical Reviews.

Vol.

No. 8/

*Shaw*

MIKELADZE, SH.

"On Numerical Integration," Dok. AN, 49, No. 3, 1945. Math. Inst. Acad. Sci., 1945-.

MIKELADZE, Sh. Ye.

"General Equation of the Elastic Line of a Beam," Dokl. AN SSSR, 50, pp. 117-19,  
1945



Mikeladze, Sh. Ye

Sh. Ye  
Mikeladze, Sh. Ye. Résolution des problèmes limites au  
moyen de la formule généralisée de MacLaurin. C. R.  
(Doklady) Acad. Sci. URSS (N.S.) 52: 753-755 (1946).  
The author shows that every linear nonhomogeneous  
equation of the form  $y^{(n)} + X_1 y^{(n-1)} + \dots + X_n y = f(x)$ , where  
the functions  $X_1, \dots, X_n$  and  $f(x)$  are continuous, can be  
reduced to a Volterra integral equation of the second kind.  
If one knows the initial values at  $x=0$ , the points of jump  
discontinuity of the solution  $y$  and its  $n-1$  derivatives and  
the magnitude of the jumps at these points.  
R. Ballman (Princeton, N. J.).

Source: Mathematical Reviews

Vol

No. 6

MIKELADZE, S. S.

PA 101

USSR/Equations, Differential  
Equations, Linear

Mar 1947

"Discontinuous Solutions for Ordinary Linear  
Differential Equations," S. E. Mikeladze, 4 pp

"CR Acad Sci" Vol LV, No 9

Theorem and mathematical proof.

8T71

MIKELADZE, Sh. Ye.

Certain Problems of Construction Mechanics

Moscow-Leningrad, 1948.

Mikelande, S. R.

Numerical integration. Uspehi Matem.  
Nauk (N.S.), no. 6(28), 1-38 (1948). (Russian)

This is an exposition of numerical differentiation and integration, with some applications to the solution of ordinary differential equations. Formulas for differentiation with and without differences are derived in the first chapter. Some sections are devoted to related topics, so that the derivations are essentially complete. Then a longer chapter is used for quadrature formulas, including formulas of Gauss, Cebyshev, and Markov, and a discussion of S. N. Bernstein's work on quadrature formulas. Sections are also devoted to integrals of the type  $\int_a^b f(x)g(x)dx$  and to Stieltjes integrals.

Quadrature formulas involving fixed ordinates are found from an interpolation formula stated to have been previously derived by the author in a book in Georgian. To get this formula, the Taylor series for  $y^{(n)}(x)$  with powers of  $x-A$ , is integrated over the interval  $(A, x)$ . When the integrand in the remainder term is replaced by Lagrange's interpolation formula, Mikelande's general formula for  $y^{(n)}(x)$  is obtained. In the third chapter, the author uses special cases of this formula to solve ordinary differential equations by a method analogous to that of Adams. Since different derivatives, differences and ordinates appear in the same quadrature formula, his method generalizes that of C. Störmer [see Bennett, Milne, and Bateman, Bull. Nat. Res. Council, no. 92 (1933), p. 82] and one attributed to A. N. Krylov. Finally, two sections are devoted to the author's iteration method for numerical integration of differential equations.

R. E. Gaskell (Ames, Iowa).

Sam

200

Source: Mathematical Reviews,

Vol 10 No. 8

Mikeladze, S. E.

Mikeladze, S. E. On the evaluation of determinants whose elements are polynomials. Akad. Nauk SSSR. Prikl. Mat. Meh. 12, 219-222 (1948). (Russian)

If  $F(\lambda)$  is the value of a determinant of order  $n$  whose elements are polynomials in  $\lambda$  then  $F(\lambda)$  is a polynomial of degree  $k$  and can be expressed in finite form by Taylor's series. The requisite coefficients  $F^{(m)}(0)$  are found by the formula  $F^{(m)}(0) = \sum_{r=0}^k A_{mr} \Delta^r F(0)$ , where  $\Delta^r F(0)$  is the  $r$ th difference obtained from  $F(0), F(1), \dots, F(k)$ . The remainder of the paper supplies the numerical values of the coefficients  $A_{mr}$  for  $m=1$  to 20,  $r=m$  to 20.

W. E. Milne (Corvallis, Ore.).

Source: Mathematical Reviews,

Vol 9 No.

10

*Smur*

MIKELADZE, Sh. Ye.

Mikeladze, S. E. Longitudinal-transverse bending of a beam on an elastic foundation. Doklady Akad. Nauk SSSR (N.S.) 59, 451-454 (1948). (Russian)

The equation of the central line of an elastic beam, resting on a yielding foundation and subjected to a constant compressive load and varying transverse load, is obtained in the form of a rapidly converging trigonometric series.

I. S. Sokolnikoff (Los Angeles, Calif.).

Source: Mathematical Reviews,

Vol 9 No. 8

Mikeladze, S. E.

Mikeladze, S. E. New quadrature formulas and their application to the integration of differential equations. 6 Doklady Akad. Nauk SSSR (N.S.) 61, 613-615 (1948). (Russian)

The author obtains by partial integration of

$$m(R_{n+1} - 1) = \int_a^b P_n(x) f^{(m)}(x) dx,$$

the general formula

$$P_n(x) = x^n + c_1 x^{n-1} + \dots$$

$$\int_a^b f(x) dx = \sum_{m=0}^n \frac{(-1)^{m-1}}{m!} [P_n^{(m)}(b) f^{(m-1)}(b) - P_n^{(m)}(a) f^{(m-1)}(a)] + R_n$$

He gives the polynomials for the quadrature formulas of Simpson, Euler-Maclaurin, Olver-Schiff and Petr and calculates the formula using the Chebyshev polynomials. A boundary problem for  $y'' = f(x)$  is solved using approximate polynomials.

J. M. Strain (Msterdam).

Source: National Review

Vol. 10, No. 5

MIKELADZE, Sh. Ye.

Mikeladze, S. E. New formulas for the numerical integration of differential equations. Doklady Akad. Nauk SSSR (N.S.) 61, 789-790 (1948). (Russian)

The interpolation formula of Newton for  $y(t)$  can be used not only with increasing abscissas  $t_1 < \dots < t_n$ , but also with zigzagging abscissas  $t_1, \dots, t_n$ . Representing  $y(a+ht)$  by the Taylor formula with the initial value  $y(a+ht_0)$  combined with a development of the integral for the remaining term according to Newton's interpolation formula with the abscissas  $a+ht_i$ , several different formulae can be obtained by permutation of the  $t_i$ . For example,  $t_0=0, t_1=1; a, a+h, \dots, a+rk$  gives  $y^{(k)}(a+h)$  expressed by  $y^{(k)}(a)$  and the mean  $k$ th order differences of  $y^{(k)}(a+ht_i)$ ,  $p \geq k; t_0=1, t_1=2; a+h, a, a+2h, \dots, a+rk$  gives  $y^{(k)}(a+2h)$ ;  $t_0=2, t_1=3; a+2h, a+h, a, a+3h, \dots, a+rk$  gives  $y^{(k)}(a+3h)$ , etc., in an analogous form. E. M. Bruins (Amsterdam)

Source: Mathematical Reviews,

Vol 10 No. 7

SMU 42



MIKELADZE, SH. E.

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USSR/Mathematics - Equations, Differential Mar 49  
Mathematics - Integrals

"Numerical Integration of Differential Equations  
With the Help of Summation Formulas," Sh. E.  
Mikeladze, 4 pp

"Dok Ak Nauk SSSR", Vol LXV, No 2

Uses repeated summations to find numerical values of  
the integral of a differential equation of form  
 $y^n = f(x, y, y', \dots, y^{n-2})$ , defined by the following  
initial conditions at  $x = a$  in the interval  $(a, X)$ :  
 $y(a) = y_0, \dots, y^{n-1}(a) = y_0^{n-1}$ . Assumes existence  
of unknown integral has been previously established.  
Submitted by Acad A. N. Kolmogorov, 29 Dec 48.

39/4956

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~~MIKELADZE, S. E.~~ MIKELADZE, S. E.

2

Mikeladze, S. E. A new method for the solution of characteristic value problems. Doklady Akad. Nauk SSSR (N.S.) 66, 353-356 (1949). (Russian)  
The author applies his method of solving linear differential equations with variable coefficients by reduction to Volterra integral equations [C. R. (Doklady) Acad. Sci. URSS (N.S.) 52, 753-755 (1946); these Rev. 8, 329] to characteristic value problems of mechanics. In particular, he discusses the transversely vibrating string with fixed ends and variable density, the linear deflection of a rod with variable axial load and one end free, a beam on an elastic support. Numerical results are given in special cases.  
M. J. Gottlieb (Chicago, Ill.).

Source: Mathematical Reviews.

Vol 1 No. 3

SMW

MIKALADZE, S. Ye.

New Method of Integration of Differential Equations," 1958.

MIKELADZE, S. E.

\*Mikeladze, S. E. *Novye metody integrirvaniya differentsial'nykh uravnenii i ih prilozheniya k zadacham teorii uprugosti.* [New methods of integration of differential equations and their application to problems in the theory of elasticity.] Gosudarstv. Izdat. Techn.-Teor. Lit., Moscow-Leningrad, 1951. 291 pp. 11.50 rubles.

This book gives numerical methods for solution of buckling and vibration problems involving columns and shafts. The principal mathematical interest lies in the first chapter on boundary problems with linear differential equations. The author sets forth here several numerical methods of finding characteristic values, most of them taken from his own writings. These methods employ numerical formulas for integration and differentiation, many of them novel or at least uncommonly used, to construct an equation for the

characteristic values of the system. In some cases, the system is converted to an integral equation, in others formulas for derivatives are used directly. Free use of unbalanced formulas is made. The chapters after the first are devoted to specific applications. The second chapter deals with buckling of columns with various types of end support and lateral restraint. No assumption as to uniformity of the cross-section is generally required. The four remaining chapters are much shorter, and deal with stability under loads distributed longitudinally, stability of curved beams, longitudinal vibrations of bars, and transverse vibrations of bars and strings.

R. E. Gaskell (Seattle, Wash.).

ms  
227

Source: Mathematical Reviews,

Vol 13 No.9

1. MIKELADZE, SH. YE.
2. USSR (600)
4. Integrals
7. Integration and differentiation under the Denjoy integral sign. Sborn AN Gruz SSR No. 7 1951.

9. Monthly List of Russian Accessions. Library of Congress. April 1951.

Mathematical Reviews  
Vol. 14 No. 7  
July - August 1953  
Analysis

Makeladze, Š. E. A new integral method of solution of boundary problems. *Sobremennyye Akad. Nauk. Gruzii* 12, 993-996 (1951). (Russian)

In order to obtain the piecewise continuous solution  $y(x)$  with piecewise continuous derivatives, of a linear differential equation the author uses a development

$$y(x) = \sum_{k=0}^n \frac{y^{(k)}(a_k)}{k!} (x - a_k)^k + \sum_{k=0}^n B_k(x - a_k)^k + \sum_{k=0}^n Q_k(x - a_k)^{k+1} + \frac{1}{(n-1)!} \int_a^b (x-t)^{n-1} y^{(n)}(t) dt$$

He substitutes in the last integral the  $n$ th derivative as given by the differential equation, eliminates, by partial integration, all derivatives of  $y(x)$  and in this way transforms boundary problems to integral equations analogous to the equation of Volterra, in the case of continuous functions.

E. M. Brauer (Bucharest)

MIKELADZE, Sh. Ya.

On the problem of the numerical solution of the system of linear differential equations with constant coefficients.

$$\dot{X} = AX, \quad X(0) = X_0$$

is solved. The system of linear differential equations with constant coefficients is solved by the method of the matrix exponential. The values of the matrix exponential having been determined, the values of the functions are computed with a Stiefens-type formula and these formulas are improved with a closed-type formula. A shorter description of a similar numerical procedure for finding characteristic values and functions follows. This article is entirely expository, reference being made to other works of the author for proofs and derivations. *R. I. Ibragimov (Sverdlovsk, USSR)*

1986. AD. 1. 1. 1. 1.

Mathematical Reviews

Vol. 11, no. 2

June 1987

Numerical and graphical

analysis

Mitcheley, S. F. Approximate formulae for multiple integrals. *Sovetskoe Radio, Mosk. Goren. SSR* 11, 193 (1986) 21-24 (1986) 1001.  
For expression the integral

$$\int \int_D f(x, y) dx dy = \sum_{i=1}^n A_i f(x_i, y_i) + R$$

in such a way that  $R$  vanishes when  $f$  is a polynomial of given degree, the author expands  $f(x, y)$  and relates the  $A_i$  to the integrals  $\int \int_D x^m y^n dx dy$  in the obvious manner. Some special consideration is given to the cases when  $D$  is a rectangle and a circle.  
— A. S. Hirschfelder

*written from the Tbilisi Pedagogical Inst im R.S. Pushkin*



MIKELADZE, Sh. Ye.

PHASE I

TREASURE ISLAND BIBLIOGRAPHICAL REPORT

AID 424 - I

Call No.: AF617879

BOOK

Author: MIKELADZE, SH. YE.

Full Title: NUMERICAL METHODS OF MATHEMATICAL ANALYSIS

Transliterated Title: Chislennyye metody matematicheskogo analiza

Publishing Data

Originating Agency: None

Publishing House: State Publishing House of Technical and  
Theoretical Literature

Date: 1953

No. pp.: 527

No. of copies: 4,000

Editorial Staff

Contributor: Kinkladze, D. A., Junior Scientific Collaborator of  
the Mathematical Institute im. A. M. Razmadze of the Academy of  
Sciences, Gruzinskaya SSR who calculated the greater part of the  
tables.

Text Data

Coverage: The table of contents fully covers the subject matter.  
The book includes 28 graphs and 115 tables. The text was compared  
with: 1) W. E. Milne's Numerical Calculus (1949); 2) J. B.  
Scarborough's Numerical Mathematical Analysis (1950); 3) J. F.  
Steffensen's Interpolation (1950); 4) J. L. Walsh's Interpolation  
and Approximation (1935); 5) E. C. Titchmarsh's The Theory of  
Functions (1932); 6) E. T. Whittaker's and G. N. Watson's A Course

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Chislennyye metody matematicheskogo analiza

AID 424 - I

in Modern Analysis (1943); and 7) E. A. Guillemin's The Mathematics of Circuit Analysis (1949). Extensive comparison reveals nothing new or not covered in the above texts.

The book appears to have the character of a compilation, as evidenced by the extensive list of references. The text tends to cover not only the subject of numerical mathematical analysis, but also topics of the general theory of functions, circuit analysis, Fourier series and operational calculus. This makes its scope of coverage unusually wide. In its definitions, deductions of formulae and laconic statements it seems to be inferior to the English texts of Scarborough, Milne and Steffensen, which are often referred to by the author in the text. A thorough knowledge of higher mathematics is a prerequisite.

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Chislennyye metody matematicheskogo analiza

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PAGES

Connection of a difference operator with a differentiation operator. General remarks.

Literature cited

514-521

Alphabetical Index

522-527

Purpose: The book is dedicated to science students and persons interested in the application of mathematics to questions of engineering.

Facilities: Mathematical Institute of the Academy of Sciences, Gruzinskaya SSR

No. of Russian and Slavic References: 48 Russian (after 1939) of a total of 162.

Available: A.I.D., Library of Congress.

10/10

Mikeladze, Sh. E.

3

✓ 629. Mikeladze, Sh. E. Numerical solution of boundary problems for ~~nonlinear~~ ordinary differential equations (in Russian); *Sobolevskii. Akad. Nauk (Urss) SSR* 14, 3, 133-137, 1963 (translated from Russian by M. D. Friedman, 872 California St., Newtonville, Mass., 6, pp.)

Author describes a procedure for the reduction of a nonlinear ordinary differential equation to a family of nonlinear algebraic equations which can be solved by conventional iterative methods. The described procedure uses numerical quadrature rather than numerical differentiation. The method is used to compute the deflection of a rod, compressed by forces exceeding the Euler critical force.

Reviewer believes that the method may be of value in certain engineering applications and should complement other well-known numerical methods for the solution of boundary-value problems. It is likely that the convergence of the method may depend on the quadrature formulas used.

G. C. Wallick, USA

Raw

MIKELADZE, Sh. Ye. Sh. Ye.

MS Mikeladze, S. E. Stability of an elastic plate of variable thickness in a uniaxial stressed state. Akad. Nauk Gruzin. SSR. Trudy Tbiliss. Mat. Inst. Razmadze 19, 211-224 (1953). (Russian. Georgian summary)

1 - F/W

A rectangular plate, whose side dimensions are  $a$  parallel to the  $x$  axis and  $b$  parallel to  $y$ , is compressed in the  $x$  direction by an arbitrary distribution of forces  $N_x$  acting along the sides parallel to  $y$ . The bending stiffness  $D$  may vary with  $y$  and may even be discontinuous in  $y$ . Assuming the form for the buckled shape  $w$  as a single wave:  $w(x, y) = f(y) \sin \pi x a^{-1}$ , the equilibrium equation and homogeneous boundary conditions on  $w$  lead to a fourth-order linear eigenvalue problem for  $f(y)$ . A general method is presented to transform the differential equation for  $f$  into an integral equation, and to obtain numerical results from the latter by finite differences and quadrature formulas. The method is demonstrated by determining the critical load for the uniform plate compressed by a uniformly distributed load ( $N_x$  and  $D$  constant) assuming that the unloaded edges are clamped.

W. Nachbar (Van Nuys, Calif.)

*[Handwritten signature]*

MIKELADZE, Sh. Ye.

USSR/Mathematics - Interpolation

1 Jun 53

"Theory of Construction of Interpolational Formulas,"  
Sh. Ye. Mikeladze, Tbilisi Math Inst, Acad Sci Georgian SSR

DAN SSSR, Vol 90, No 4, pp 503-506

Develops interpolational formulas, with differences  
of the function  $y^{(n)}(x)$  of various kinds, from the

$$\text{eq } y(a+ht) = \sum_{k=0}^{n-1} (T-t)^k (h^k/k!) y^{(k)}(a+ht) + h^n/(n-1)!$$

$$\int_t^T (T-t)^{n-1} y^{(n)}(a+xh) dx, \text{ namely, by expanding}$$

254T91

$y^{(n)}(x)=f(x)$  in the differences  $f(a)$ ,  $\nabla f(a)$ , ...,  $\nabla^p f(a) = \Delta^p f(a-ph)$ ,  $\Delta^{p+1} f(a-ph)$ , etc. Presented by  
Acad A. N. Kolmogorov 2 Apr 53.

USSR/Mathematics - Finite

Differences

21 Sep 53

"Expansion of the Finite Difference of a Function  
in the Differences of its Derivative," Sh.Ye.  
Mikeladze, Math Inst, Acad Sci Georgian SSR

DAN SSSR, Vol 92, No 3, pp 479-482

Outlines a method for constructing the expansions  
of a function in the differences of its deriva-  
tive. States that particular results were ob-  
tained earlier by M.F. Subbotin (Byul Sredneaz  
Gos Un-ta [Bull of Central Asia State Univ], No 16,  
273 (1942); No 17, 21 (1928) [sic] and 20 years

268T80

later by W.G. Bickley using symbolic methods  
(J Math and Phys (Mass), 27, 3, 191 (1948)).  
Presented by Acad A.N. Kolmogorov 20 Jul 53.

268T80

MIKELADZE, S. F.

Mikeldze, S. F. Remarks on the theory of discontinuous solutions of ordinary differential equations. Soobsh. Akad. Nauk Gruzin. SSR 15 (1954), 647-654. (Russian)

Let  $Ly=0$  be a linear ordinary differential equation with continuous coefficient. The author has given [C. R. (Dokl.) Acad. Sci. URSS (N.S.) 55 (1947), 789-792; MR 9, 36] an expression in terms of a fundamental set of solutions for a solution with jump discontinuities in  $y^{(k)}$  ( $k=0, \dots, n-1$ ). Here he first extends this expression to cover the case (P) in which the coefficients depend also continuously on an arbitrary number of parameters. Next he discusses a boundary-value problem for a self-adjoint second-order equation, concluding that in case (P) the proper values of the parameters cannot be determined for a solution with assigned discontinuities, without supplementary conditions. The final section treats special equations soluble in closed form.

F. A. Ficken.

MIKELADZE, Sh. Ye.

USSR/Mathematics - Approximate solution of Cauchy problem

FD-663

Card 1/1 : Pub. 85 - 18/20

Author : Mikeladze, Sh. Ye. (Tbilisi)

Title : Approximate solution of the Cauchy problem

Periodical : Prikl. mat. i mekh., 18, 244-249, Mar/Apr 1954

Abstract : Solves approximately the Cauchy problem for general nonlinear differential equations with initial data differentiable sufficient number of times. Refers to his book Chislennyye metody matematicheskogo analiza [Numerical methods of mathematical analysis], GITTL, 1953.

Institution : --

Submitted : December 17, 1953



Mikeladze, Sh. Ye.

Sh. Ye.

Mikeladze, ~~Sh. Ye.~~ On discontinuous solutions of ordinary quasi-differential equations. Dokl. Akad. Nauk SSSR (N.S.) 105 (1955), 641-644. (Russian)  
The equations are of the form

$$Ly = q_0 \frac{d}{dx} q_1 \frac{d}{dx} \dots q_{n-1} \frac{d}{dx} q_n y + p y = 0,$$

where the coefficients are continuous functions of  $(x, \alpha, \beta, \dots)$  ( $\alpha, \beta, \dots$  parameters) in a region including the interval  $a \leq x \leq b$ . The quasi-derivatives of  $y$  are defined thus:  $y^{(0)} = p_n y$ ,

$$y^{(n-k)} = q_k \frac{d}{dx} q_{k+1} \frac{d}{dx} \dots q_{n-1} \frac{d}{dx} q_n y \quad (k=1, \dots, n-1).$$

First a "fundamental" set of solutions is constructed at  $x=s$ . Then it is shown how to form a linear combination having, along with its quasi-derivatives, desired jumps at specified points in  $[a, b]$ . Next a solution is found for the nonhomogeneous equation  $Ly = q(x, \alpha, \beta, \dots)$ . In conclusion, certain special cases are noted. F. A. Ficken.

VAL'FISH, A.Z., redaktor; MANDZHAVIDZE, G.F., redaktor; MIKELADZE, Sh.Ye.,  
redaktor; MUSKHELISHVILI, N.I., otvetstvennyy redaktor; CHELIDZE, V.G.,  
redaktor; CHOGOSHVILI, G.S., redaktor; KARACHKOV, S.R., tekhnicheskii  
redaktor.

[Linear discontinuous boundary problems of the function theory,  
singular integral equations and some of their applications] Lineinye  
razryvnye granichnye zadachi teorii funktsii, singuliarnye integral'nye  
uravneniia i nekotorye ikh prilozheniia. Tiflis, Izd-vo Akademii nauk  
Gruz.SSR. 1956. 158 p. (Akademia nauk Gruz.SSR. Matematischeskii institut.  
Trudy, vol. 23)

(MLRA 10:5)

(Functions, Discontinuous)

(Integral equations)

(Functions of complex variables)

SOV/137-57-6-9439

Translation from Referativnyy zhurnal, Metallurgiya, 1957, Nr 6, p 18 USSR.

AUTHOR: Mikeladze, (No initials given)

TITLE: G N Nikoladze and the Didube Pilot Plant (G N Nikoladze : didubyskiy opytnyy zavod) in Georgian

PERIODICAL: Tr Gruz politekhn in-t, 1956, Nr 1 (42), pp 29-34

ABSTRACT A discussion is presented of the role of Prof. Georgiy Nikolovich Nikoladze in the design, construction, and breaking in of the Zestafoni Ferromanganese Plant using Chiatura ores. A pilot plant with an 1125 kva 3-phase electric furnace was built in Tbilisi (Didube) in 1928 under Nikoladze's guidance to determine the technical procedures and other indices of production and economics. The following questions were studied: 1) Choice of the best reductant for electric melting of ferromanganese by comparison of Tkviluli coals and Donbass coke; 2) use of limestone as flux instead of burnt lime; 3) the comparative economics of various ores from the Chiatura mine; 4) optimum granulation of the charge components; and 5) the effect of the working voltage on the smelting process, etc.

Card 1/1

Z.Kh.

MIKELADZE, Sh.Ye.

On a review and remark following it. Usp.mat.nauk 11 no.3:241-242  
My-Je '56. (MIRA 9:9)  
(Calculus) (Zhukov, A.I.)

MIKELADZE, Sh. Ye.

sh. Ye. 14 16  
Mikeladze, Sh. Ye. Numerical integration of differential equations in the complex plane. Soobsh. Akad. Nauk Gruzii: SSR 17 (1956), 97-102. (Russian)

The author uses the same type of quadrature formulas, applicable in the real case, to integrate numerically an ordinary differential equation of second order along some straight line in the complex plane. He also indicates the use of such methods for analytic continuation.

W. E. Milne (Corvallis, Ore.)

MIKELADZE Sh. Ye.

✓ Mikeladze, S. E. Quadrature formulas for a regular function. Soobsh. Akad. Nauk Gruzii. SSR 17 (1956), 289-296 (Russian)

I-FW

For an analytic function  $f(z)$  of a complex variable the author gives a general quadrature formula of type

$$(*) \quad \int_a^{a+H} f(z) dz = H \sum_{j=1}^n A_j f(a+t_j H) + R_n$$

Assuming (\*) is exact ( $R_n=0$ ) for polynomials of degree  $n$ , the  $A_j$  may be derived by integrating the Lagrange interpolation polynomial, or by undetermined coefficients. For various fixed points  $(a+t_j H)$  the author derives known quadrature formulas of Salzer [J. Math. Phys. 29 (1950), 96-104; MR 12, 56], Birkhoff and Young [ibid. 29 (1950), 217-221; MR 12, 445], and Young [ibid. 31 (1952), 22-44; MR 13, 782, 1140]. If  $f(z)$  is real for real  $z$ , the author takes equal weights  $A_j$  and finds formulas of the Chebyshev type.

$$(*) \quad \int_a^{a+H} f(z) dz = \frac{2}{H} \sum_{j=1}^n \operatorname{Re} f(z_j)$$

1/2

MIKE LADZE, S.E.

exact for polynomials of degree  $n$ . A numerical example with  $f(x) = e^{-x}$  and  $n = 10$  yields accuracy to 6 significant decimals.

New quadrature formulas are found with the points  $a + ih$ , at the center and vertices of regular polygons. Also, one for  $\int_H f(x) dx$  is given in terms of  $f(0)$ ,  $f(\pm H)$ ,  $f(\pm 2H)$ ,  $f(\pm iH)$ , and  $f(\pm 2iH)$ .

G. E. Forsyth.

1-FW

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**Mikelande, S. E.** Approximate formulas for the multiple integrals of a regular function. *Soviet. Akad. Nauk. Gruzia SSR* 17 (1956), 577-584. (Russian)

The point of departure is the reduction in the complex field of multiple integrals to single integrals by the formula:

$$(*) \int_1^z \dots \int_1^z w^{(n)}(z) dz^n = ((n-1)!)^{-1} \int_1^z (z-u)^{n-1} w^{(n)}(u) du.$$

The author then uses ideas developed in an earlier paper [same *Soviet. Akad. Nauk. Gruzia SSR* 17 (1956), 289-296; *MR* 18, 479] to give methods of obtaining numerical integration formulas for the right side of (\*), and hence for the left side of (\*).

Formulas of both closed and open type are considered. In illustration the author gives numerical formulas for integrating  $w' = dw/dz = f(z, w)$ ,  $w'' = f(z, w, w')$ , and  $w' = f(z, w)$  over a network in a complex region.

G. E. Forsythe (Stanford, Calif.)



MIKELADZE, S.E.

✓ Mikeladze, S. E. Formulas of mechanical quadratures for multiple integrals. Akad. Nauk Gruz. SSR. Trudy Tbiliss. Mat. Inst. Razmadze 22 (1956), 277-299. (Russian)

1-F/W

The special results cannot be summarized in a short space but the method is of interest. The relation to multiple integrals is incidental and occurs through the formula

$$\int_{x_0}^{x_1} \int_{x_2}^{x_3} \dots \int_{x_m}^{x_{m+1}} f(x) dx = \frac{h^k}{(k-1)!} \int_{-1}^1 (1-t)^{k-1} / (a+th) dt,$$

where  $a = \frac{1}{2}(x_0 + x_1)$ ,  $h = \frac{1}{2}(x_1 - x_0)$ . After stating this the author considers integrals such as  $\int_0^1 p(x)/(x) dx$ , first with finite limits, then with one or both limits infinite. In the latter cases  $p$  is taken to contain an exponential factor.

For  $a$  and  $b$  finite, the endeavor is to express the integral either, in the usual way, as a linear combination of the values of  $f$  at selected points, or else as a linear combination of its divided differences, and in either case to the highest possible order of accuracy. The method stems from the observation that if  $x_1, x_2, \dots, x_m$  are zeros of a polynomial  $P_m(x)$  of degree  $m$  of the set of polynomials orthogonal with respect to the weight  $p(x)$ , and if  $f(x)$  is expanded as a series in its divided differences

$$f(x_1), f(x_1, x_2), \dots, f(x_1, x_2, \dots, x_m), f(x_1, x_2, \dots, x_m, x_1), \dots,$$

1/2

then when the series is substituted into the integral certain terms disappear as a result of the orthogonality. A simple extension of the notion permits treatment of cases where a limited number of relations are imposed upon the  $x_i$ , e.g. that certain ones are fixed.

A. S. Householder (Madison, Wis.).

2

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MIKELADZE, Sh.Ye.

Review and accompanying remarks. Trudy Mat.inst.AN Grus.SSR 22:319-  
338 '56. (MLRA 10:3)  
(Numerical calculations) (Mathematics)

Mikeladze, S. E.

✓ Mikeladze, S. E. Numerical solution of the inhomogeneous polyharmonic equation. Inžen. Sb. 23 (1956), 190-202. (Russian)

The solution of the boundary value problem for the polyharmonic equation is discussed by the method of various types of grids. The existence and uniqueness of the solution of the linear system of simultaneous equations which are used to replace the partial differential equation are proved and the convergence of the solution of the approximate problem to the exact solution is discussed.

C. Saltzer (Syracuse, N.Y.)

2  
1-F/W

MIKELADZE, Sh. Ye.

Quadratic formulas for multiple integrals having the highest degree of precision. Soob. AN Gruz. SSR 18 no.1:3-10 Ja '57.

(MLRA 10:5)

1. Akademiya nauk Gruzinskoy SSR, Tbilisskiy matematicheskiy institut im. A.M. Razmadze. 2. Tbilisskiy gosudarstvennyy universitet imeni Stalina. Chlen-korrespondent Akademii nauk Gruzinskoy SSR.

(Integrals, Multiple)

MIKELADZE, Sh.Ye.

Numerical differentiation in the complex region. Soob. AN  
Gruz.SSR 18 no.4:385-392 Ap '57. (MLBA 10:7)

1. Akademiya nauk Gruzinskoy SSR, Tbilisskiy matematicheskiy  
institut im. A.M.Razmadze. Chlen-korrespondent Akademii nauk  
Gruzinskoy SSR.

(Functional analysis) (Integral equations)  
(Differential equations)

MIKELADZE, Sh.Ye.

Approximate solution of the system of nonlinear equations.  
Soob. AN Gruz. SSR 20 no.6:647-653 Je '58. (MIRA 11:10)

1. AN Gruzinskoy SSR, Tbilisskiy matematicheskiy institut im. A.M.  
Razmadze i Tbilisskiy gosudarstvennyy universitet imeni Stalina.  
Chlen-korrespondent AN Gruzinskoy SSR.  
(Differential equations)

MIKELADZE, Sh.Ye.

Some iterations of higher orders. Soob. AN Gruz. SSR 22 no.3:  
257-264 Mr '59. (MIRA 12:8)

1. AN Gruz SSR, Tbilisskiy matematicheskiy institut im. A.M.  
Razmadze i Tbilisskiy gosudarstvennyy universitet im. Stalina,  
chlen-korrespondent AN Gruz SSR.  
(Integrals)



MIKELADZE, Sh.Ye.

General method for the numerical solution of differential equations. Soob.AN Gruz.SSR 22 no.5:513-518 My '59.

(MIRA 12:11)

1. Akademiya nauk Gruzinskoy SSR; Tbilisskiy matematicheskiy institut im. A.M.Razmadze; Tbilisskiy gosudarstvennyy universitet imeni Stalina, chlen-korrespondent AN Gruzinskoy SSR.  
(Differential equations)

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J, 044/61, 000/008, 036 039  
0111/0333

AUTHOR: Mikeladze, Sh. Ye.  
TITLE: The method of parameter variation for the solution of equations  
PERIODICAL: Referativnyy zhurnal, Matematika, no. 8, 1961, 17, abstract 8V237 ("Soobsnch. AN Gruz SSR", 1959, 42, no. 1, 3-9)  
TEXT: The author considers the equation

$$z = \sum_{\nu=0}^m a_{\nu} f_{\nu}(z) \quad (1)$$

where the functions  $f_{\nu}(z)$  are regular in the domain  $D$  containing the simple root  $z = \alpha$  of (1), and  $a_{\nu}$  are imaginary numbers. In auxiliary functions  $f_{\nu}(z)$  with vanishing coefficients  $a_{\nu}$  are introduced into the equation (1):

Card 1/3

The method of parameter variation for

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$$z = \sum_{\nu=0}^p a_{\nu} f_{\nu}(z)$$

where it is assumed that the auxiliary functions are different from zero in the point  $z$ . The author understands the  $a_{\nu}$  as independent variables, differentiates (1) with respect to these variables and obtains an iteration formula for the solution of (1). In the case of the variation of one coefficient  $a_k$  this formula has the form:

$$z = \varphi(z) \equiv z - \xi(z) \omega(z)$$

where

$$\omega(z) = \sum_{\nu=0}^m a_{\nu} f_{\nu}'(z) - z,$$

$$\xi(z) = \frac{f_k(z)}{(\omega(z)f_k'(z) - \omega(z)f_k'(z))_k}$$

$$f_k'(\infty) \neq 0$$

Card 2/2

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The method of parameter variation for  
Since  $\varphi'(x) = 0$ , the iteration process converges in a certain neighborhood of  $\infty$  if the initial approximation  $z_0$  lies in this neighborhood. In the case  $f(z) = \text{const}$  one obtains the known iteration formula of Newton. As special case for  $z=x$ ,  $m=1$ ,  $a_0=a_1=1$ ,  $f_0(x)=x$ ,  $f_1(x)=f(x)$  one obtains for the solution of the equation  $f(x)=0$  the iteration formula

$$x_n = \left[ 1 + \frac{f(x_{n-1})}{f(x_{n-1}) - x_{n-1} f'(x_{n-1})} \right] x_{n-1}$$

it is applicable where Newton's formula becomes senseless. An iteration formula for determining the zeros of a polynomial is given, also for the case that all zeros are real and simple. Numerical examples are given.

[Abstracter's note: Complete translation.]

Card 3/3

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C111/0111

63510

AUTHOR: Mikeladze, Sh. Ye.  
TITLE: Boundary value and eigenvalue problems for quasidifferential equations

PERIODICAL: Referativnyi zhurnal. Matematika, 1961, 41, abstract 48113 ("Tr. Tbilissk. gos. univ. AN SSSR", 1961, 26, 24-26)

TEXT: The author considers the quasidifferential equation

$$\sum_{n=0}^{\infty} \frac{d^n u}{dx^{n+1}} + \sum_{n=0}^{\infty} \frac{d^n u}{dx^{n+2}} + \sum_{n=0}^{\infty} \frac{d^n u}{dx^{n+1}} + \dots = 0$$

The quasidifferential equation is defined. There are generalizations of the definition given by the author (Mikeladze Sh. Ye., Nekotoryye zadachi teorii mekhaniki [Some problems of structural mechanics] GITTL, 1961). Methods for determining the mentioned

Boundary value and eigenvalue

solutions are discussed. As an example the author considers the equation of an elastic beam of variable cross section.

[Abstracter's note: Complete translation]

Part 1

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C111/C333

AUTHOR: Mikeladze, Sh Ye

TITLE: Numerical solution of ordinary differential equations with the aid of polynomials

PERIODICAL: Referativnyy zhurnal, Matematika, no 8, 1961, 30-31.  
abstract 8V208 ("Tr Tbilisis matem in-ta AN Gruz SSR" 1959, 26, 263-284)

TEXT: For the solution of the Cauchy problems, boundary value problems and eigenvalue problems the author proposes a method consisting in reducing the differential equations to systems of algebraic or transcendental equations with the aid of the polynomials of Bernshteyn. Here the theorem of S. N. Bernshteyn on the uniform approximation on  $[0,1]$  of a continuous function  $y(x)$  by polynomials

$$\sum_{s=0}^p A_s(x) y\left(\frac{s}{p}\right) \quad (p \geq 1), \quad (1)$$

where  $A_s(x) = \binom{p}{s} x^s (1-x)^{p-s}$ , is essentially used, as well as the Card 1/4

Numerical solution of ordinary . . .

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C111/C333

theorem on uniform approximation on  $[0,1]$  of the continuous derivatives of  $y(x)$  by the derivatives of corresponding order of the polynomials  
(\*) In the case of an equation of first order

$$y' = f(x,y) \quad (2)$$

with the initial condition  $y(0) = 0$  the polynomial  $y'(x) = \sum_{s=0}^p A'_s(x) y(\frac{s}{p})$

is substituted into (2) and  $x$  is replaced by  $x = s/p$  ( $s = 0, 1, \dots, p$ ); this leads to the system of  $p+1$  equations with the  $p$  unknowns  $y_s = y(s/p)$ :

$$A_0(\frac{s}{p}) y_0 + A_1(\frac{s}{p}) y_1 + \dots + A_p(\frac{s}{p}) y_p = f(\frac{s}{p}, y_s)$$

It is shown that this system contains  $p$  equations with a coefficient determinant different from zero. The proposed method is also applicable to systems of differential equations and to differential equations of order  $n$ . An equation of second order is considered as example. In the case of boundary value problems (for a system or for an equation of order  $n$ ) the boundary conditions must be taken into account for the

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Numerical solution of ordinary

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C111/C333

set-up of the linear system. The application of the method to eigenvalue problems is explained by the example of the differential equation

$$y^{(n)} + X_1(x, \lambda) y^{(n-1)} + \dots + X_n(x, \lambda) y = X(x, \lambda)$$

with the boundary conditions

$$\sum_{k=0}^{n-1} \alpha_{ki} y^{(k)}(0) + \sum_{k=0}^{n-1} \beta_{ki} y^{(k)}(1) = \gamma_i$$

$$(i = 1, 2, \dots, m \geq n).$$

Here the coefficients  $\alpha_{ki}$ ,  $\beta_{ki}$  can also depend on  $\lambda$ ; assume that  $X_1, \dots, X_n, X, \alpha_{ki}, \beta_{ki}$  and the  $\gamma_i$  are unique and continuous with respect to  $x$  and  $\lambda$  in a certain domain of the space  $(x, \lambda)$ . In the equation and in the boundary conditions the function and its derivatives are replaced according to the formula

$$y^{(k)}(x) = \sum_{s=0}^p A_s^{(k)}(x) y \left( \frac{s}{p} \right)$$

Card 3/4

Numerical solution of ordinary . . .

S/044/61,000,008,029,039  
C111/C333

the corresponding  $x$ -values are chosen from the interval  $[0,1]$  and one obtains a homogeneous system of equations. If its determinant is put equal to 0, then one obtains an equation for the determination of the sought eigenvalues  $\lambda$ . As an example the author considers the problem  $y'' + \lambda xy = 0$ ,  $y(0) = y(1) = 0$ . He describes the application of the proposed method to Volterra integral equations of second kind, to Fredholm integral equations and to some integro-differential equations. At the end of the paper there are given tables of the values of the polynomials  $A_g(x)$  and of their derivatives  $A_g^{(k)}(x)$  ( $k = 0,1, \dots, 4$ ;  $g = 0,1, \dots, 10$ ) for  $\lambda \cdot g/10$  ( $g = 0,1, \dots, 10$ ).  
[Abstracter's note: Complete translation.]

Card 4/4

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S. 683/60/027 010.001 1.1  
B\*12/B\*38

AUTHOR: Mikeladze, Sh. Ye  
TITLE: Numerical solution of the equation of heat conduction  
SOURCE: Akademiya nauk Gruzinskoy SSR Matematicheskyy ...  
Trudy, v. 21, 1960, 367 - 410

TEXT: The author investigates two methods of solving the equation  $\partial u / \partial t = a^2 \partial^2 u / \partial x^2$  numerically (and more general equations of the same type). Applying the first method he replaces this equation by the following system of difference equations:  
 $U_{i,k+1} = (1 - 2/\lambda)U_{i,k} + (U_{i-1,k} + U_{i+1,k})/\lambda$ . The second method is algebraic: The equation  $\partial u / \partial t = a^2 \partial^2 u / \partial x^2$  is replaced by  
 $(6 - \lambda)U(x - h, t + \tau) = (12 + 10\lambda)U(x, t) + (2 - 6 - \lambda)U(x + h, t) + (6 - \lambda)U(x - h, t) + (12 - 10\lambda)U(x, t) + (2 + \lambda)U(x + h, t)$   
( $\lambda = h^2/a^2 \tau \neq 6$ ). For both methods formulas are derived for error estimation. The author compares his results with those of other authors P. P. Yushkov (Trudy instituta energetiki AN Belorusskoy SSR, vyp. 6, M., 1957).

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B112/B118

Numerical solution of the equation of

1984; Trudy Leningradskogo Instituta khimicheskoy promyshlennosti, 1984; Prikladnaya matematika i mekhanika, 12, 1946, and D. Yu. Panyov, Spravochnik po chislennomu resheniyu differentsial'nykh uravneniy v chastnykh proizvodnykh. Handbook for the numerical solution of partial differential equations, M. - L., 1968, are referred to. There are 2 figures, 3 tables, and 24 references: 19 Soviet and 5 non-Soviet. The four references to English-language publications read as follows: L. F. Richardson, The approximate arithmetical solution by finite differences of physical problems involving differential equations with an application to the stresses in a masonry dam, Philosoph. Trans. R. Soc. London, Ser. A, vol. 210, 1927; Kaj L. Nielsen, Methods in numerical analysis, The Macmillan Company, New York, 1964; W. E. Milne, Numerical solution of differential equations, John Wiley Sons, Inc. New York, 1954; Andrew D. Booth, Numerical methods, Butterworths Scientific Publications, London, 1957.

REMITTED: December 1981

Card 1

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